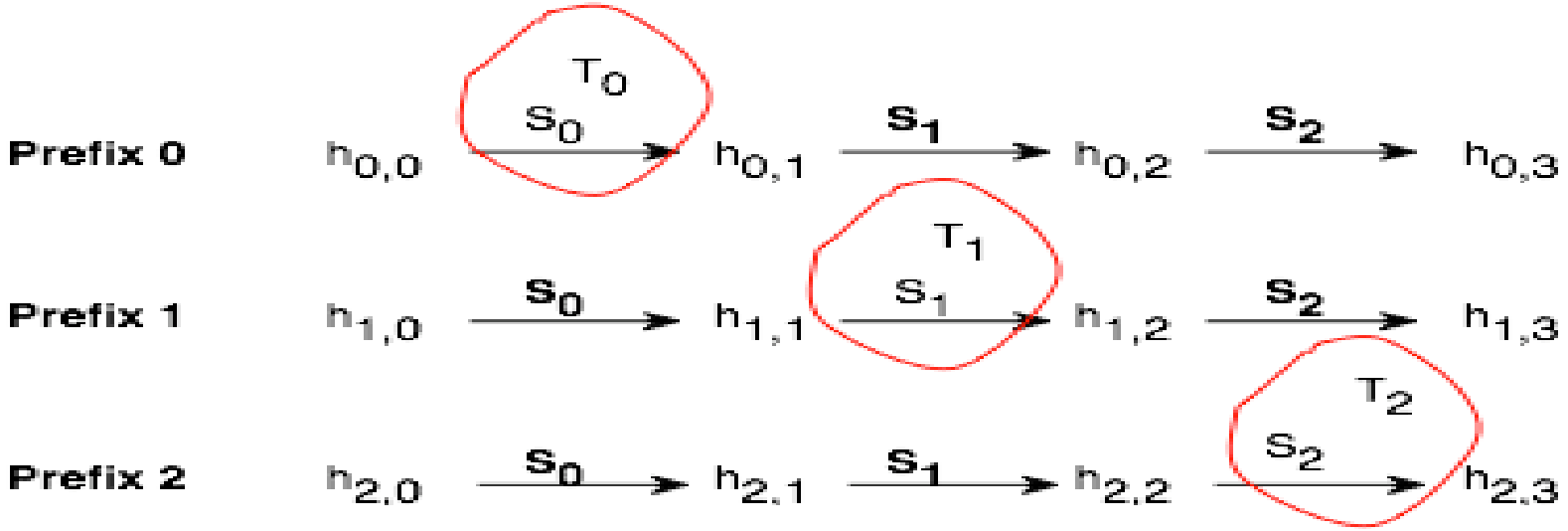
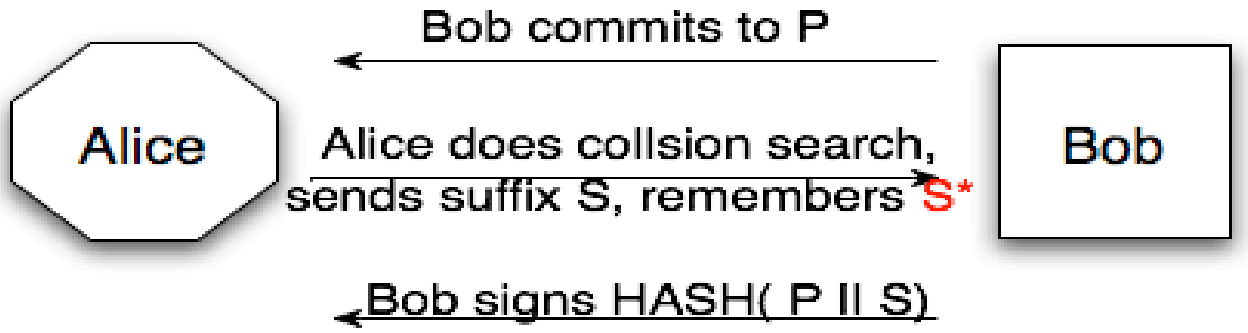
Trojan Messages: Collisions with an unknown prefix



Elena Andreeva, Charles Bouillaguet, Orr Dunkelmann, Pierre-Alain Fouque, Jonathan J. Hoch, **John Kelsey**, Adi Shamir, and Sebastien Zimmer

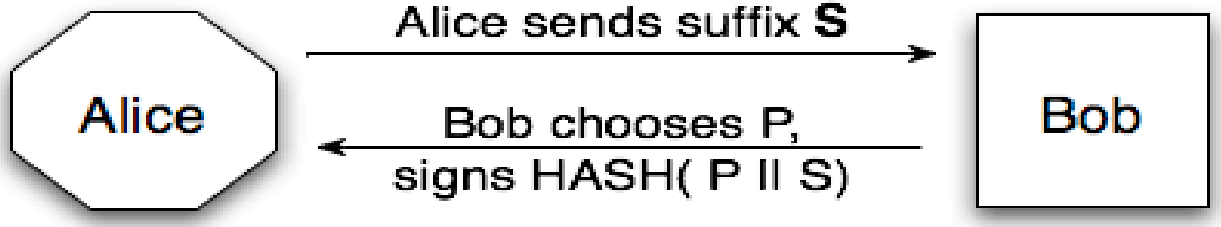
Alice can break our hash….

UNSAFE: Alice commits to suffix after she knows prefix



Alice CAN cheat Bob--she knows
collision for HASH(P II S)

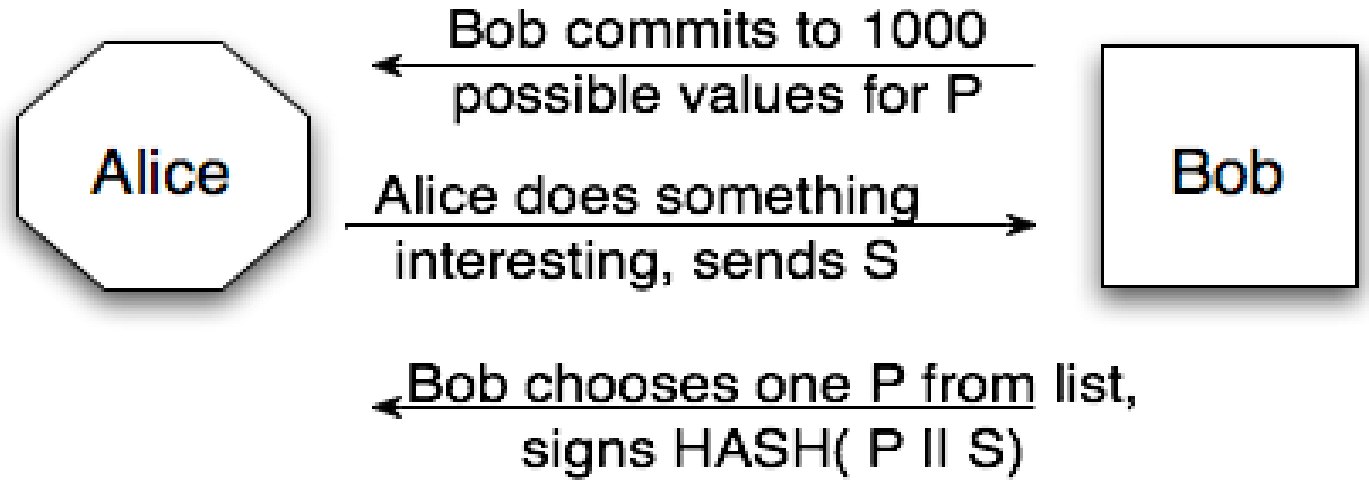
SAFE: Alice commits to suffix before she knows prefix



Alice can't cheat Bob--she doesn't know
collisions for HASH(P II S)

This Result

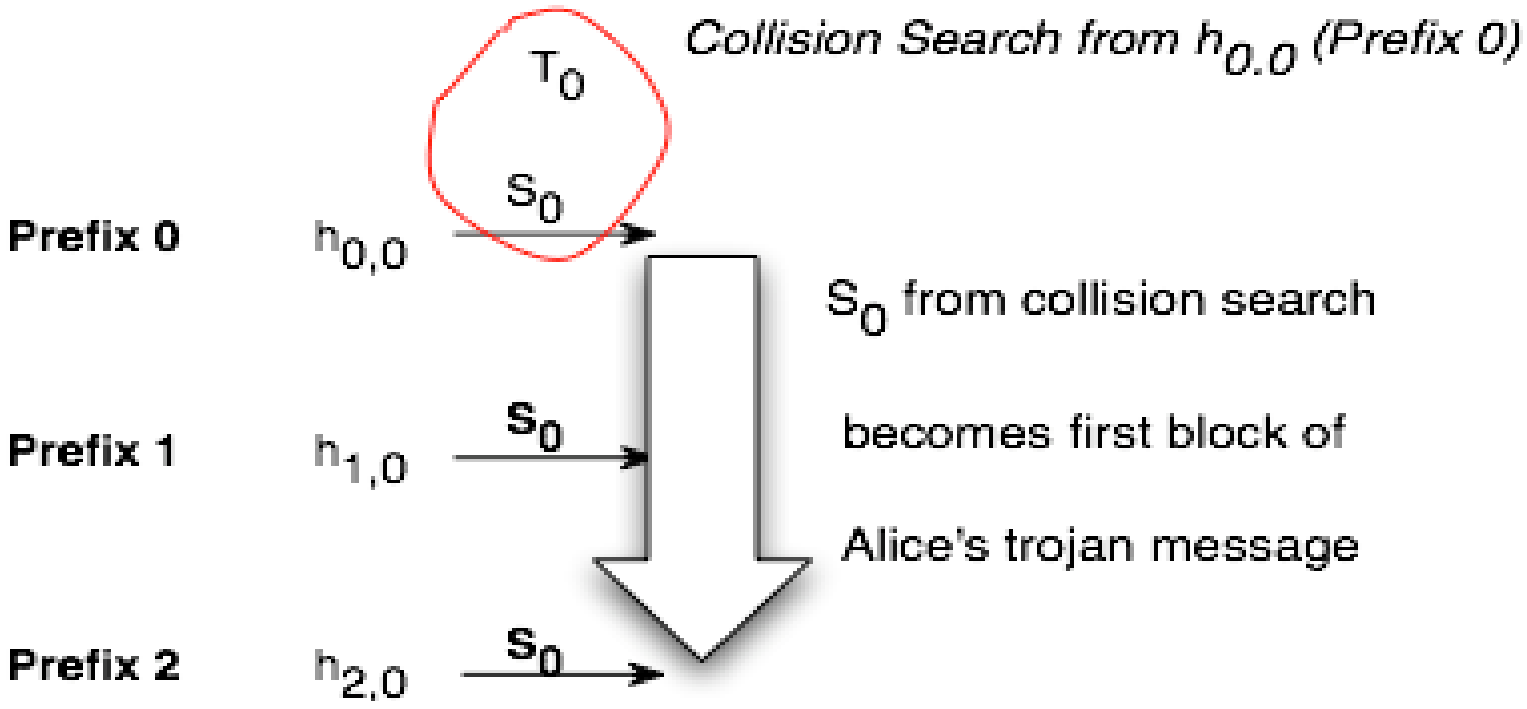
ALSO UNSAFE: Bob commits to a list of values for P



Alice CAN cheat Bob--she knows collision
for HASH(P II S) for every P in list!

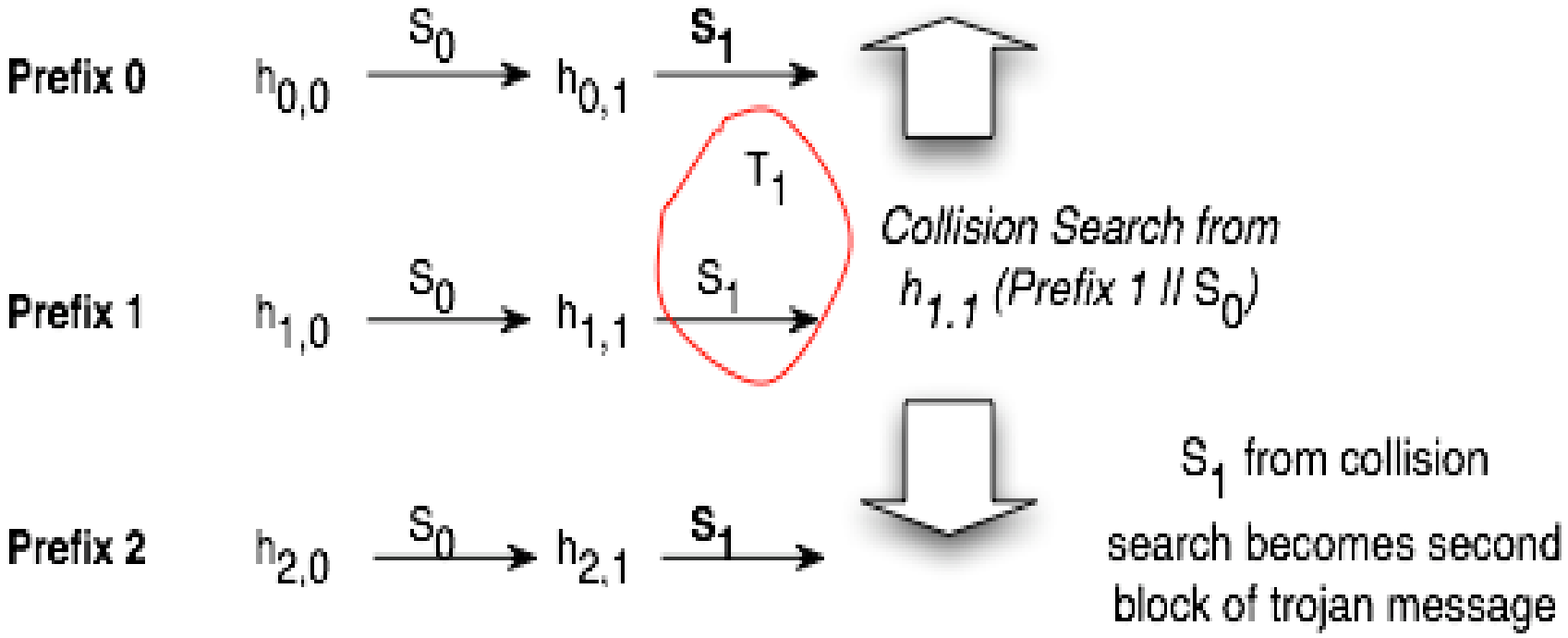
Scales linearly: N possible prefixes -->

N block suffix, requiring N collision searches



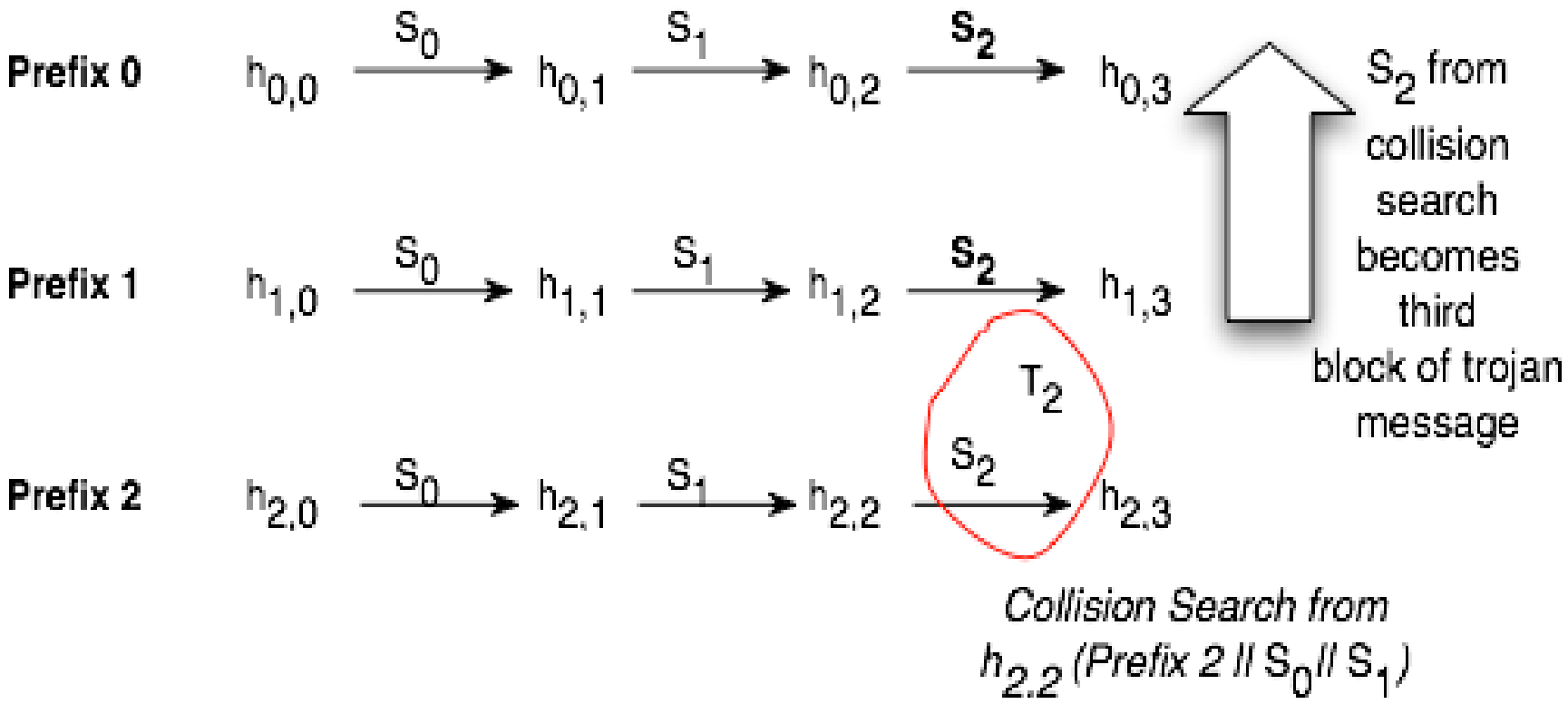
- Do first collision search from Prefix 0
  - (starting from $h_{0,0}$)
  - Search yields S_0, T_0
  - S[0] becomes first block of Trojan message
  - Alice remembers T_0 in case Bob uses Prefix 0

Trojan message so far: ***S_0.***



- Do next collision search from Prefix 1
  - (starting from $h_{1,1}$)
  - Search yields S_1, T_1
  - S_1 becomes next block of Trojan message
  - Alice remembers T_1 in case Bob uses Prefix 1

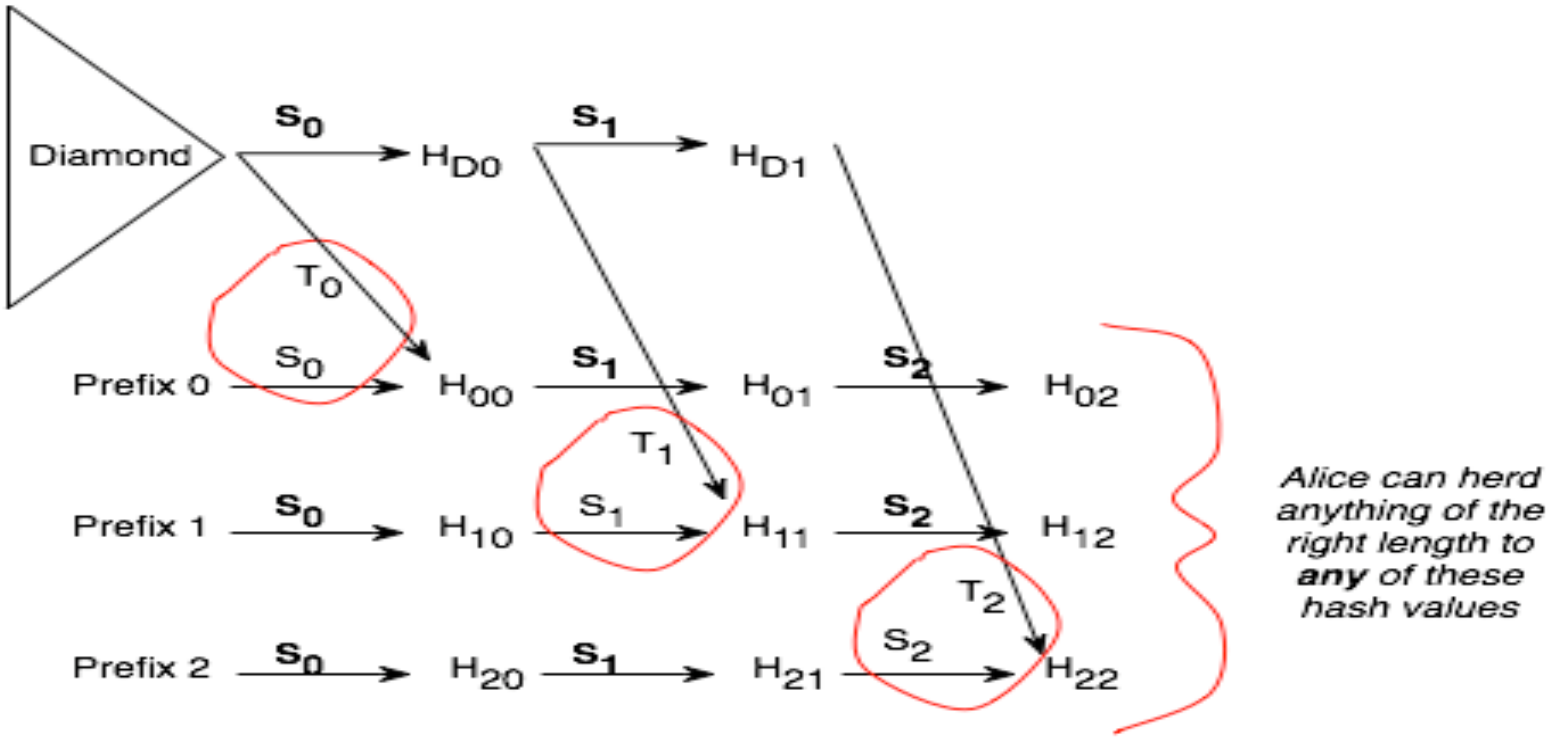
Trojan message so far: $S_0 \,||\, S_1$

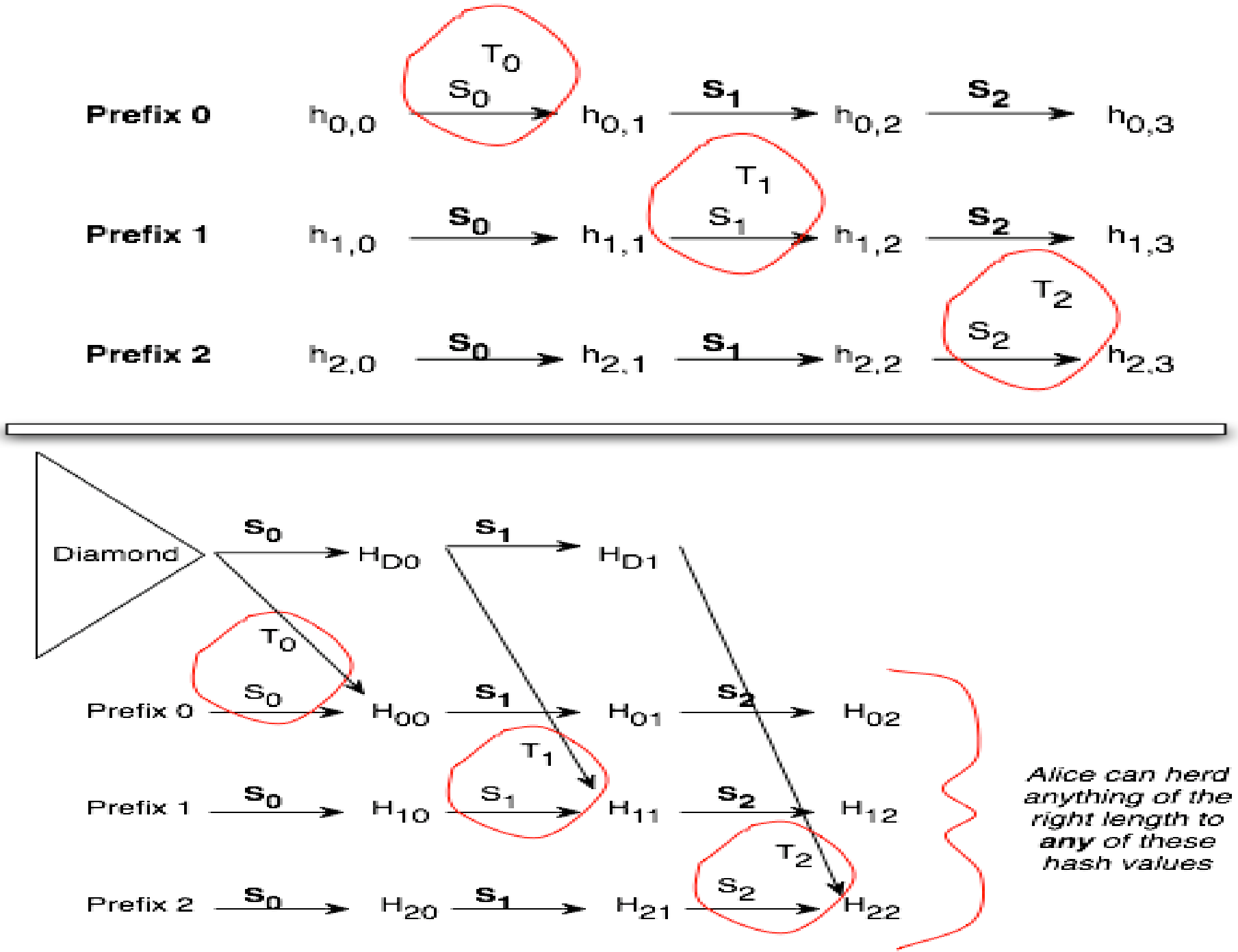


- Next collision search:
  - Starting from **Prefix 2|| S_0 || S_1** (starting from $h_{2,2}$)
  - Search yields S_2, T_2
  - S_2 becomes final block of Trojan message
  - Alice remembers T_2 in case Bob uses Prefix 2

Final Trojan message: $S = S_0 \,||\, S_1 \,||\, S_2$

- Herding Variant
  - Bob commits to N prefixes
  - Alice builds diamond, sends S
  - Bob chooses P
  - Alice can herd any prefix to HASH(P || S)




Prefix 0
Prefix 1
Prefix 2
$h_{0,0}$
$h_{0,1}$
$h_{0,2}$
$h_{0,3}$
$h_{1,0}$
$h_{1,1}$
$h_{1,2}$
$h_{1,3}$
$h_{2,0}$
$h_{2,1}$
$h_{2,2}$
$h_{2,3}$
T_0
S_0
S_1
S_2
T_1
T_2
Diamond
H_{D0}
H_{D1}
H_{00}
H_{01}
H_{02}
H_{10}
H_{11}
H_{12}
H_{20}
H_{21}
H_{22}
Alice can herd anything of the right length to any of these hash values